

# Harnessing the Sun's Gravity for LEO to GEO Transfers

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The geosynchronous orbit (GEO) belt is in incredibly high demand, yet it requires a considerable amount of fuel to reach. Common launch sites for GEO satellites include Guiana Space Centre, Kennedy Space Center and Baikonur Cosmodrome. Without dog-leg maneuvers, the minimum inclination that may be reached are 5, 28.5 and 51° respectively. Therefore, for high latitude launch sites, a large part of the fuel budget is allocated for inclination changes ( $\Delta i$ ). To minimize this additional cost, several strategies have been developed in the past, such as two-burn strategies where the  $\Delta i$  is optimally distributed over the two burns, three-burn bi-elliptic or super-synchronous transfers where the  $\Delta i$  is performed at high altitudes, etc.

In [1], a new strategy is proposed where the  $\Delta i$  and periaresis raise ( $\Delta r_p$ ) from LEO to GEO is performed by third-body perturbations from the Sun. Transfers starting at a 51° inclined orbit have been found that require only 2.5% more  $\Delta V$  than transfers from 28.5°. Hence, this technology facilitates flexibility in launch site selection to go to GEO. Such transfers depart LEO after an in-plane impulse in the velocity-direction to reach the required transfer orbit eccentricity and arrive back at periaresis at GEO altitude with the right inclination, after which another in-plane impulse in the anti-velocity direction re-circularises the orbit. Assuming the initial  $r_p$  and  $i$  are fixed, the design variables are time of year of launch, initial transfer eccentricity ( $e$ ), argument of periaresis ( $\omega$ ) and longitude of ascending node ( $\Omega$ ). Every permutation of those four design variables result in different realizations for final  $r_p$  and final  $i$ . Given the size of the state space, and the sensitive maps between design variables and final  $r_p$  and  $i$  values, navigating the state space is not trivial.

In this paper, a robust way to find transfers for any time of year and initial orbit inclination is developed. For each time of year, with resolution one day, the combination of initial  $e$ ,  $\omega$  and  $\Omega$  that satisfy the required  $\Delta i$  and  $\Delta r_p$  are determined for an orbit with 51° initial  $i$ . This means

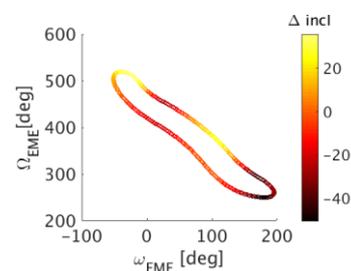


Fig. 1. Example  $\Delta r_p$  contour

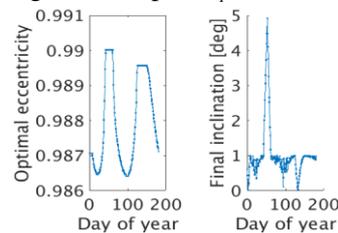


Fig. 2. Final results

finding intersections between contour lines representing the correct  $\Delta r_p$  and correct  $\Delta i$ , at the smallest  $e$  they occur. By minimizing  $e$ , the required fuel to inject the spacecraft from LEO into its transfer orbit is minimized.

The utilized method consists of two main steps. First of all, for a certain  $e$ , using a tangent-predictor, pseudo-arc length-corrector scheme [2], the required  $\Delta r_p$  contour shape is traced out [3]. An example of this can be found in Fig. 1. It has been observed that each of these contour shapes has four local minima of final  $i$ . The second step utilizes a slightly different predictor-corrector scheme to trace out the path of the four local minima on the  $\Delta r_p$  contour shapes through different values of  $e$ , without having to compute the entire  $\Delta r_p$  contour shapes. This step is repeated until a point has been found for which the final inclination is close to zero or a maximum  $e$  of 0.99 is reached. Finally, the design variables ( $e, \omega, \Omega$ ) for the four local optima can be fed to the next day. This allows us to skip the first step and immediately trace out the minimum  $i$  on the contour surfaces. The lowest final  $i$  of the four families and its  $e$  are plotted in Fig. 2 for half a year.

## References

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